

$$\int \left(e^{3x} \operatorname{sen}(2x) + \frac{x}{x-2} \right) dx =$$

Utilizzando i metodi di scomposizione e parti

$$\int e^{3x} \operatorname{sen}(2x) dx + \int \frac{x}{x-2} dx = \frac{1}{3} \int 3e^{3x} \operatorname{sen}(2x) dx + \int \frac{x-2+2}{x-2} dx =$$

$$" = \frac{1}{3} \left[e^{3x} \operatorname{sen}(2x) - 2 \int e^{3x} \cos(2x) dx \right] + \int \frac{x-2}{x-2} dx + \int \frac{2}{x-2} dx =$$

$$" = \frac{1}{3} e^{3x} \operatorname{sen}(2x) - \frac{2}{3} \int e^{3x} \cos(2x) dx + x + 2 \ln|x-2| + c$$

$$" = \frac{1}{3} e^{3x} \operatorname{sen}(2x) - \frac{2}{9} \left[e^{3x} \cos(2x) + 2 \int e^{3x} \operatorname{sen}(2x) dx \right] + x + 2 \ln|x-2| + c$$

$$\int e^{3x} \operatorname{sen}(2x) dx + \int \frac{x}{x-2} dx = \frac{1}{3} e^{3x} \operatorname{sen}(2x) - \frac{2}{9} e^{3x} \cos(2x) - \frac{4}{9} \int e^{3x} \operatorname{sen}(2x) dx + x + 2 \ln|x-2| + c$$

$$\frac{13}{9} \int e^{3x} \operatorname{sen}(2x) dx + \int \frac{x}{x-2} dx = \frac{1}{3} e^{3x} \operatorname{sen}(2x) - \frac{2}{9} e^{3x} \cos(2x) + x + 2 \ln|x-2| + c$$

$$\int e^{3x} \operatorname{sen}(2x) dx + \int \frac{x}{x-2} dx = \frac{3}{13} e^{3x} \operatorname{sen}(2x) - \frac{2}{13} e^{3x} \cos(2x) + x + 2 \ln|x-2| + c$$